

# Densities and Solubilities for Binary Systems of Carbon Dioxide + Water and Carbon Dioxide + Brine at 59 °C and Pressures to 29 MPa

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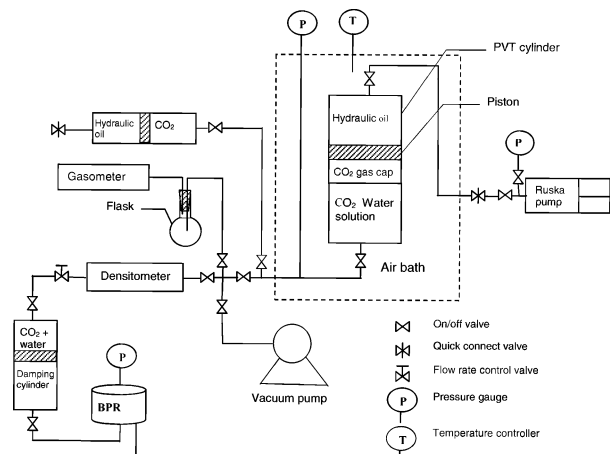
Densities and solubilities for binary systems of carbon dioxide + water and carbon dioxide + Weyburn-formation brine were measured at a temperature of 59 °C and pressures up to 29 MPa. Density values were obtained for both the saturated and unsaturated aqueous carbon dioxide solutions at different pressures. A correlation in the literature was used to predict the solubility of carbon dioxide in the aqueous phase, and the results were compared with the measured data. The measured density of aqueous carbon dioxide solutions was correlated as a function of carbon dioxide concentration and pressure. A simple method for determining the density of aqueous carbon dioxide solutions was recommended.

## Introduction

The increase of CO<sub>2</sub> concentration in the atmosphere has been considered one of the greatest factors of global warming. To mitigate the accumulation of CO<sub>2</sub> in the atmosphere, CO<sub>2</sub> capture and storage have been widely investigated since the early 1990s. The two most promising options for CO<sub>2</sub> storage are in depleted oil and gas reservoirs and in deep oceans. The solubility of CO<sub>2</sub> in aqueous solution and the density of aqueous CO<sub>2</sub> solution as a function of pressure are important phase behavior data required for modeling CO<sub>2</sub> sequestration and migration in reservoirs or oceans. In addition, these data are very useful in the simulation of CO<sub>2</sub>-related enhanced oil recovery processes. Other applications may also be found in chemical and environmental engineering.

Different from most of the other gases, the dissolution of CO<sub>2</sub> in aqueous solution under most reservoir or deep-ocean conditions results in an increase in density of the solution, which can induce a natural convection. On the basis of this phenomenon, Haugan and Drange<sup>1</sup> proposed a CO<sub>2</sub> sequestration method in the deep ocean by a shallow CO<sub>2</sub> injection in the upper 200–400 m of the ocean. For CO<sub>2</sub> sequestration in depleted oil reservoirs, the density-induced natural convection needs to be investigated in order to make a better prediction of the CO<sub>2</sub> migration process underground. Therefore, the density data of CO<sub>2</sub>-formation water is essential to the prediction.

Some results for the density of aqueous CO<sub>2</sub> solutions have been reported under deep ocean conditions: CO<sub>2</sub> + seawater at 3 °C and 35 MPa by Ohsumi et al.;<sup>2</sup> CO<sub>2</sub> + water at 5–20 °C and 6.44–29.49 MPa by Teng and Yamasaki<sup>3</sup>. Parkinson and Nevers<sup>4</sup> reported the densities of CO<sub>2</sub> + water solutions in a temperature range from 4.95 °C to 40.55 °C and pressures up to 3.4 MPa. More recently, Yaginuma et al.<sup>5</sup> measured the densities of CO<sub>2</sub> + distilled water at 31 °C and pressures up to 10 MPa. However, for the density of CO<sub>2</sub> + formation brine solutions under practical reservoir conditions (high pressure, elevated temperature, and various salinities) more experimental measurements are required. The solubilities of CO<sub>2</sub> in



**Figure 1.** Schematic diagram of experimental apparatus.

water or synthetic brine (NaCl and CaCl<sub>2</sub> solutions) under different conditions were reported by many researchers.<sup>3,6–10</sup> Recently, results of CO<sub>2</sub> solubility in a variety of aqueous solutions were reported.<sup>11–14</sup> These solutions are mainly used in the processing industry and are quite different from reservoir brines. Experimental measurements are still needed for CO<sub>2</sub> solubility in reservoir brine samples in order to examine the reliability of the available correlations under reservoir conditions.

This paper reports the experimental results of CO<sub>2</sub> solubilities in deionized water and an oil reservoir formation brine as a function of pressure and the densities of these aqueous CO<sub>2</sub> solutions as a function of both CO<sub>2</sub> concentration and pressure. The pressure covered in the measurements ranged from 0.3 MPa to 29 MPa. All measurements were made at 59 °C, the temperature of Weyburn reservoir where an International Energy Agency Weyburn CO<sub>2</sub> monitoring and storage project is underway.

## Experimental Section

**Apparatus.** A schematic diagram of the experimental apparatus is shown in Figure 1. This apparatus is similar to a pressure–volume–temperature (PVT) test system. It mainly consists of a 500-cm<sup>3</sup> PVT cylinder, a high-pressure CO<sub>2</sub> cylinder, a high-pressure Ruska pump, a back pressure regulator (BPR), a densitometer, and a gasometer.

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**Table 1. Analysis of Weyburn Formation Brine Sample**

density/(g·cm <sup>-3</sup> ) at 22 °C	1.0619
at 59 °C	1.0459
total dissolved solids/(mg·L <sup>-1</sup> )	92950
calcium/(mg·L <sup>-1</sup> )	1970
sodium/(mg·L <sup>-1</sup> )	29140
magnesium/(mg·L <sup>-1</sup> )	566
potassium/(mg·L <sup>-1</sup> )	454
iron/(mg·L <sup>-1</sup> )	<0.2
chloride/(mg·L <sup>-1</sup> )	52640
sulfate/(mg·L <sup>-1</sup> )	3800
pH at 20 °C	7.67

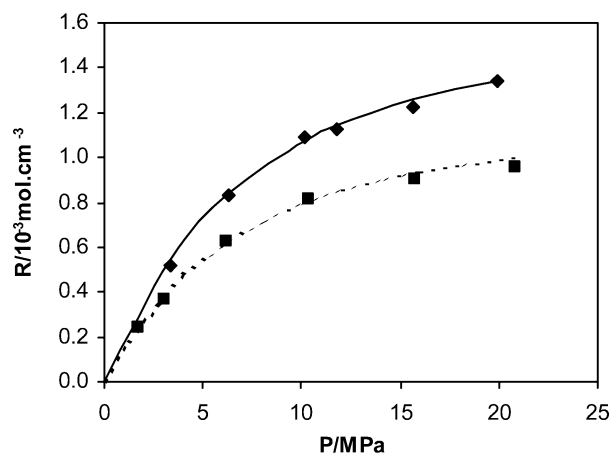
**Table 2. Solubility of CO<sub>2</sub> in Deionized Water at 59 °C**

P/MPa	CO <sub>2</sub> solubility/(10 <sup>-3</sup> mol·cm <sup>-3</sup> )		
	measured	predicted	relative error (%)
19.89	1.344	1.337	0.49
15.62	1.227	1.256	2.34
11.76	1.127	1.142	1.31
10.14	1.089	1.074	1.43
6.27	0.835	0.838	0.34
3.34	0.514	0.546	5.83

The PVT cylinder was used to equilibrate the CO<sub>2</sub> and the aqueous solution. It was placed in an air bath and can be rocked to speed up the equilibration between the CO<sub>2</sub> and the aqueous solution. The temperature of the air bath was controlled within ±0.5 °C of the desired value. The pressure of the cylinder was monitored by a Heise pressure gauge (Dresser Instrument) with an accuracy of ±0.025% of the full-scale span (34.5 MPa). The high-pressure CO<sub>2</sub> cylinder was used to contain the prepressurized CO<sub>2</sub>. The Ruska pump was used to pressurize and transfer fluids. The BPR was connected to the densitometer through a damping cylinder. This was used to keep the pressure of the system constant when transferring the saturated aqueous CO<sub>2</sub> solutions from the PVT cylinder to the densitometer. Density was measured using a DMA 512P (Anton Paar) vibrating-tube densitometer with a repeatability of ±1 × 10<sup>-5</sup> g·cm<sup>-3</sup>. The temperature in density measurement was controlled within ±0.2 °C by the circulating oil bath. The Ruska gasometer combined with a flask was employed to determine the CO<sub>2</sub>-to-water ratio of the solution.

**Procedures.** Before starting a test, approximately 450 cm<sup>3</sup> of water sample was introduced into the PVT cylinder. Prior to adding CO<sub>2</sub> into the cylinder, the density of the water sample was measured at different pressures up to 29 MPa. Then the pressure was reduced to a lower level, and CO<sub>2</sub> was injected. The minimum amount of CO<sub>2</sub> needed for a test was estimated using the Chang et al.<sup>15</sup> correlation. To make sure that there was a gas cap at equilibrium, 30% more CO<sub>2</sub> than the estimated amount was added to the PVT cylinder. After the fluids in the PVT cylinder were pressurized up to a desired pressure, the cylinder was rocked frequently to accelerate the dissolving process. When the cylinder pressure stayed constant over a period of more than 5 h, the equilibrium between the CO<sub>2</sub> phase and the aqueous phase was considered to be reached.

Once the equilibrium was achieved at a given pressure, about 20 cm<sup>3</sup> of CO<sub>2</sub> + water solution was transferred to the densitometer under a pressure which was 5–10 kPa higher than the saturation (or equilibrium) pressure with an assistance of the BPR. The density of CO<sub>2</sub> + water solution was first measured at the saturation pressure. Then the densities of the same CO<sub>2</sub> aqueous solution at elevated pressures were determined. These measurements gave the densities of the aqueous solution under different pressures (at and above saturation pressures) for a constant CO<sub>2</sub> concentration.

**Figure 2.** Solubility of CO<sub>2</sub>,  $R$ , in deionized water and Weyburn brine vs pressure at 59 °C. ♦, Deionized water, measured; ■, brine, measured; solid line, deionized water, predicted; dashed line, brine, predicted.**Table 3. Solubility of CO<sub>2</sub> in Weyburn Brine at 59 °C**

P/MPa	CO <sub>2</sub> solubility/(10 <sup>-3</sup> mol·cm <sup>-3</sup> )		
	measured	predicted	relative error (%)
20.87	0.958	1.002	4.37
15.72	0.905	0.934	3.10
10.38	0.814	0.805	1.09
6.20	0.626	0.618	1.32
3.01	0.367	0.374	1.83
1.76	0.240	0.239	0.18

**Table 4. Values of Coefficients in Equations 4–6**

	$i = 0$	$i = 1$	$i = 2$	$i = 3$	$i = 4$
$a_i$	1.163	-16.630	111.073	-376.859	524.889
$b_i$	0.965	-0.272	0.0923	-0.1008	0.0998
$c_i$	1.280	-10.757	52.696	-222.395	462.672

Another 20 cm<sup>3</sup> solution was released from the PVT cylinder to the atmospheric pressure to determine the CO<sub>2</sub> solubility in aqueous phase at the saturation pressure. The liquid was collected in the flask, and its mass was measured. The evolved CO<sub>2</sub> was collected in the gasometer, where its volume was determined at ambient conditions. The atmospheric pressure was 101.2 ± 0.1 kPa in all measurements. From the mass of the liquid and the volume of the CO<sub>2</sub>, the solubility of CO<sub>2</sub> in aqueous solution at the saturation pressure and test temperature was calculated from the following equation

$$R = \frac{n_g}{(m_g + m_w)/\rho_s} \quad (1)$$

where  $R$  is the solubility of CO<sub>2</sub> in aqueous phase,  $n_g$  and  $m_g$  are the number of moles and mass of CO<sub>2</sub>, respectively,  $m_w$  is the mass of water, and  $\rho_s$  is the density of aqueous CO<sub>2</sub> solution at the saturation pressure.  $n_g$  is calculated from the measured gas volume using the equation of state, and  $m_g$  is the product of  $n_g$  and the molecular weight of CO<sub>2</sub>. It should be noted that this technique of measuring solubility of CO<sub>2</sub> is suitable for nearly neutral aqueous solutions, such as most reservoir brines, but may not be sufficient when the pH value of water sample is high. For the latter case, the reaction between CO<sub>2</sub> and the aqueous solution has to be considered.

The PVT equilibrium measurements were started from a high saturation pressure. After the first measurement, the pressure in the PVT cylinder was lowered to the next

**Table 5. Densities of CO<sub>2</sub> + Deionized Water Solutions at 59 °C**

P/MPa	$\rho/(\text{g}\cdot\text{cm}^{-3})^a$	P/MPa	$\rho/(\text{g}\cdot\text{cm}^{-3})$	P/MPa	$\rho/(\text{g}\cdot\text{cm}^{-3})$	P/MPa	$\rho/(\text{g}\cdot\text{cm}^{-3})$	P/MPa	$\rho/(\text{g}\cdot\text{cm}^{-3})$	P/MPa	$\rho/(\text{g}\cdot\text{cm}^{-3})$	P/MPa	$\rho/(\text{g}\cdot\text{cm}^{-3})$
		<b>3.34</b>	<b>0.9905</b>	<b>6.27</b>	<b>0.9947</b>	<b>10.14</b>	<b>0.9989</b>	<b>11.76</b>	<b>1.0002</b>	<b>15.62</b>	<b>1.0031</b>	<b>19.89</b>	<b>1.0059</b>
0.45	0.9845	8.03	0.993	10.34	0.9968	13.56	1.0008	13.46	1.0013	17.43	1.0039	22.09	1.007
1.48	0.9851	11.85	0.995	14.99	0.9993	17.34	1.0028	18.90	1.0043	21.06	1.0059	24.67	1.0083
3.69	0.9863	18.10	0.9983	20.09	1.002	19.62	1.004	22.93	1.0064	24.32	1.0076	28.59	1.0103
7.31	0.9883	28.00	1.0034	27.77	1.0062	27.34	1.008	28.18	1.009	28.13	1.0095		
11.90	0.9907												
19.83	0.9948												
28.62	0.9993												

<sup>a</sup> Density of deionized water without CO<sub>2</sub>.

level. The above procedure was repeated until the measurement at the desired lowest saturation pressure was finished.

The maximum uncertainty in pressure measurements is less than  $\pm 0.009$  MPa. The accuracy of the evolved gas volume measurements (from about 144 cm<sup>3</sup> up to 477 cm<sup>3</sup>) is  $\pm 1$  cm<sup>3</sup> (or the maximum relative uncertainty is 0.7%). The accuracy in the mass measurements of water (from about 10 g up to 30 g) is 0.01 g (or the maximum relative uncertainty is 0.1%). The maximum relative uncertainty for the solubility determined from eq 1 is estimated to be less than 2%. The maximum uncertainty in density measurements is estimated within  $\pm 1 \times 10^{-4}$  g·cm<sup>-3</sup>.

## Results and Discussion

In this work, solubilities of CO<sub>2</sub> in deionized water and an oil reservoir formation brine were determined at a temperature of 59 °C and pressures up to 20 MPa. The densities of CO<sub>2</sub> + deionized water and CO<sub>2</sub> + brine solutions were determined as a function of both CO<sub>2</sub> concentration and pressure. The brine sample was collected from the Weyburn reservoir, Saskatchewan, Canada. Its analysis was presented in Table 1. The CO<sub>2</sub> used was supplied by Canadian Liquid Air Ltd. with a purity of 99.99%.

**CO<sub>2</sub> Solubility in Deionized Water and Brine.** The measured solubilities of CO<sub>2</sub> in deionized water and brine at different pressures are listed in Tables 2 and 3, respectively. These results are presented graphically in Figure 2. The CO<sub>2</sub> solubility vs saturation pressure curves in Figure 2 show that: (1) the solubility of CO<sub>2</sub> in both deionized water and brine increased with pressure; (2) the increase in CO<sub>2</sub> solubility with pressure became less as the pressure increased; (3) the salinity reduced the CO<sub>2</sub> solubility in brine compared with that in deionized water. The CO<sub>2</sub> solubility in Weyburn brine was about 30% lower than that in deionized water at the highest saturation pressure tested.

Several correlations given in the literature<sup>10,15,16</sup> for predicting the solubility of CO<sub>2</sub> in the aqueous phase were examined in this work. The correlation by Chang et al.<sup>15</sup> was found to be more reliable than others when used under reservoir conditions and easier to be applied in reservoir simulation since all the dissolved substances are lumped together as a salinity. This correlation was developed by fitting the experimental data from different researchers.<sup>6,8,9,17</sup>

For CO<sub>2</sub> solubility in water  $R_w$ , the correlation of Chang et al.<sup>15</sup> is given as

$$R_w = 1.152^{-3} a P \left[ 1 - b \sin \left( \frac{\pi}{2} \frac{145cP}{145cP + 1} \right) \right] \quad \text{for } P < P^0/145 \quad (2)$$

$$R_w = 1.152^{-3} [R_w^0 + m(145P - P^0)] \quad \text{for } P \geq P^0/145 \quad (3)$$

where the solubility  $R_w$  is in mol·cm<sup>-3</sup>, and  $P$  is the total

pressure of CO<sub>2</sub> and water in MPa.  $a$ ,  $b$ ,  $c$ ,  $P^0$ ,  $R_w^0$ , and  $m$  are functions of temperature  $T$  and they are given as

$$a = \sum_{i=0}^4 (a_i \times 10^{-3i}) \left( \frac{9}{5} T + 32 \right)^i \quad (4)$$

$$b = \sum_{i=0}^4 (b_i \times 10^{-3i}) \left( \frac{9}{5} T + 32 \right)^i \quad (5)$$

$$c = 10^{-3} \sum_{i=0}^4 (c_i \times 10^{-3i}) \left( \frac{9}{5} T + 32 \right)^i \quad (6)$$

$$P^0 = \frac{2}{\pi} \frac{\sin^{-1}(b^2)}{c \left[ 1 - \frac{2}{\pi} \sin^{-1}(b^2) \right]} \quad (7)$$

$$R_w^0 = a P^0 (1 - b^3) \quad (8)$$

$$m = a \left\{ 1 - b \left[ \sin \left( \frac{\pi}{2} \frac{c P^0}{c P^0 + 1} \right) + \frac{\pi}{2} \frac{c P^0}{(c P^0 + 1)^2} \cos \left( \frac{\pi}{2} \frac{c P^0}{c P^0 + 1} \right) \right] \right\} \quad (9)$$

where the temperature  $T$  is in °C. The forms of eqs 2–6 are different from the original ones given in ref 15 as a result of unit conversion. Values of coefficients  $a_i$ ,  $b_i$ , and  $c_i$  in eqs 4–6 are shown in Table 4. For the temperature of 59 °C used in this work,  $P^0/145$  was calculated to be 35.5 MPa. Since the maximum pressure of the measurements in this work was lower than 35.5 MPa, eq 2 was used in solubility predictions.

The solubility of CO<sub>2</sub> in brine,  $R_b$ , is calculated as<sup>15</sup>

$$R_b = 10^{-\{0.028S\}/\{(9/5)T+32\}^{0.12}} R_w \quad (10)$$

where  $R_b$  is in mol·cm<sup>-3</sup>.  $S$  is the salinity of brine, which is defined as the total dissolved salts in the solution in mass percent.<sup>18</sup>

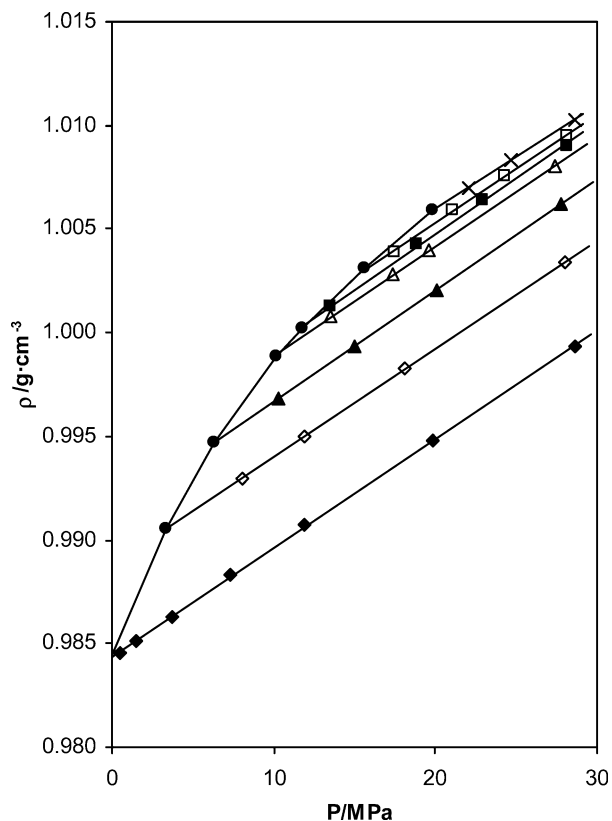
The predicted results from eqs 2 and 10 are also listed in Tables 2 and 3 and plotted in Figure 2. The salinity for Weyburn brine was 8.36 mass %, which was used in eq 10. Comparison between the calculated results and the determined data shows that the Chang et al.<sup>15</sup> correlation can give a satisfactory prediction for CO<sub>2</sub> solubility in both deionized water and formation brine.

**Density of Aqueous CO<sub>2</sub> Solution.** Measured densities for CO<sub>2</sub> + deionized water and CO<sub>2</sub> + brine solutions are listed in Tables 5 and 6, respectively. In both Tables 5 and 6, the data in the first row (in bold) are the densities at the saturation pressure conditions. The data in the first set of Tables of 5 and 6 are pressures and densities for deionized water and brine, respectively, without dissolution of CO<sub>2</sub>. These results are also plotted as a function of pressure for different CO<sub>2</sub> concentrations in Figures 3 and 4, respectively. In these two figures, the curves with solid

**Table 6. Densities of CO<sub>2</sub> + Weyburn Brine Solutions at 59 °C**

P/MPa	$\rho/(\text{g}\cdot\text{cm}^{-3})^a$	P/MPa	$\rho/(\text{g}\cdot\text{cm}^{-3})$	P/MPa	$\rho/(\text{g}\cdot\text{cm}^{-3})$	P/MPa	$\rho/(\text{g}\cdot\text{cm}^{-3})$	P/MPa	$\rho/(\text{g}\cdot\text{cm}^{-3})$	P/MPa	$\rho/(\text{g}\cdot\text{cm}^{-3})$	P/MPa	$\rho/(\text{g}\cdot\text{cm}^{-3})$
		<b>1.76</b>	<b>1.0484</b>	<b>3.01</b>	<b>1.0497</b>	<b>6.20</b>	<b>1.0534</b>	<b>10.38</b>	<b>1.0562</b>	<b>15.73</b>	<b>1.0596</b>	<b>20.87</b>	<b>1.0628</b>
0.24	1.046	6.58	1.0507	10.54	1.0534	10.14	1.0555	14.29	1.0581	18.96	1.0613	24.38	1.0646
0.83	1.0463	15.17	1.055	14.14	1.0552	13.89	1.0574	17.55	1.0599	20.83	1.0624	25.96	1.0655
2.27	1.0471	22.85	1.0588	22.03	1.0591	20.86	1.0609	21.84	1.0621	24.27	1.0642	27.69	1.0666
6.32	1.0491	28.64	1.0616	28.64	1.0623	28.46	1.0648	27.83	1.0651	27.62	1.066		
10.79	1.0513												
18.67	1.0552												
24.52	1.058												
28.93	1.0601												

<sup>a</sup> Density of Weyburn brine without CO<sub>2</sub>.

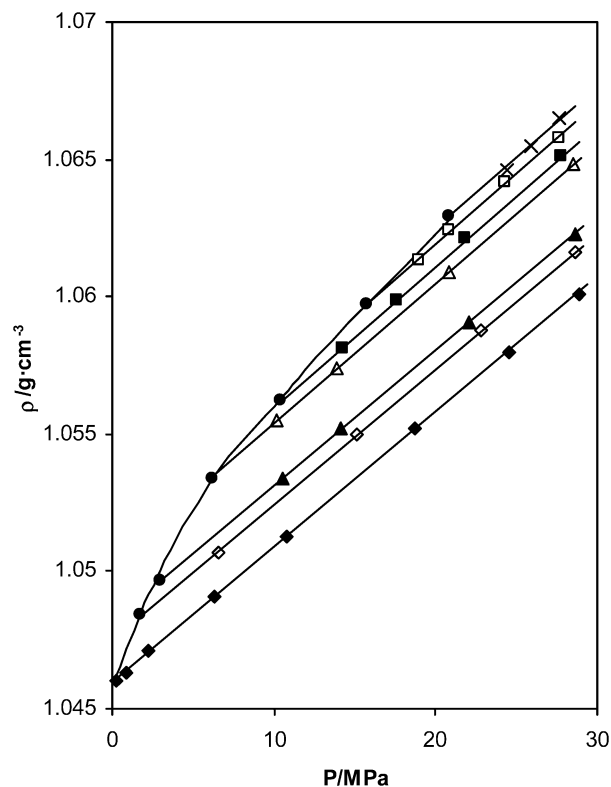


**Figure 3.** Density of CO<sub>2</sub> + deionized water solution vs pressure with different CO<sub>2</sub> concentrations at 59 °C.  $\blacklozenge$ , deionized water,  $C = 0$ ;  $\diamond$ ,  $C = 0.24 \times 10^{-3} \text{ mol}\cdot\text{cm}^{-3}$ ;  $\blacktriangle$ ,  $C = 0.835 \times 10^{-3} \text{ mol}\cdot\text{cm}^{-3}$ ;  $\triangle$ ,  $C = 1.089 \times 10^{-3} \text{ mol}\cdot\text{cm}^{-3}$ ;  $\blacksquare$ ,  $C = 1.127 \times 10^{-3} \text{ mol}\cdot\text{cm}^{-3}$ ;  $\square$ ,  $C = 1.227 \times 10^{-3} \text{ mol}\cdot\text{cm}^{-3}$ ;  $\times$ ,  $C = 1.344 \times 10^{-3} \text{ mol}\cdot\text{cm}^{-3}$ ;  $\bullet$ , at different saturation pressures.

diamonds represent the densities of the aqueous phase without CO<sub>2</sub> (or at zero CO<sub>2</sub> concentration), the curves with solid circles represent the densities of CO<sub>2</sub> saturated aqueous solutions at different saturation pressures, and the rest of the curves represent the densities of unsaturated solutions at different CO<sub>2</sub> concentrations,  $C$ .

As shown in Figures 3 and 4, for a given CO<sub>2</sub> concentration, the density of the solution for both deionized water and brine increased linearly with pressure. All these curves had the same slope as that of the aqueous phase at zero CO<sub>2</sub> concentration within experimental errors. For a constant pressure, the density of aqueous solution increased with CO<sub>2</sub> concentration. In other words, the dissolution of CO<sub>2</sub> in both deionized water and brine increased the density of the aqueous phase.

In Figures 5 and 6, the density of aqueous CO<sub>2</sub> solutions at selected pressures was plotted as a function of CO<sub>2</sub> concentration for the CO<sub>2</sub> + deionized water and CO<sub>2</sub> + brine systems, respectively. In these two figures, the



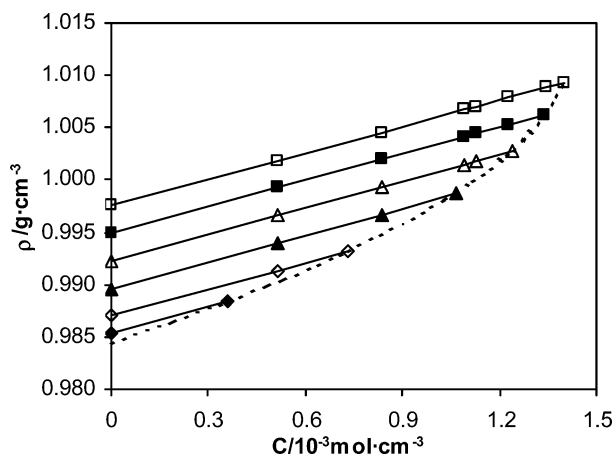
**Figure 4.** Density of CO<sub>2</sub> + Weyburn brine solution vs pressure with different CO<sub>2</sub> concentrations at 59 °C.  $\blacklozenge$ , Weyburn brine,  $C = 0$ ;  $\diamond$ ,  $C = 0.24 \times 10^{-3} \text{ mol}\cdot\text{cm}^{-3}$ ;  $\blacktriangle$ ,  $C = 0.367 \times 10^{-3} \text{ mol}\cdot\text{cm}^{-3}$ ;  $\triangle$ ,  $C = 0.626 \times 10^{-3} \text{ mol}\cdot\text{cm}^{-3}$ ;  $\blacksquare$ ,  $C = 0.814 \times 10^{-3} \text{ mol}\cdot\text{cm}^{-3}$ ;  $\square$ ,  $C = 0.905 \times 10^{-3} \text{ mol}\cdot\text{cm}^{-3}$ ;  $\times$ ,  $C = 0.958 \times 10^{-3} \text{ mol}\cdot\text{cm}^{-3}$ ;  $\bullet$ , at different saturation pressures.

intercept of each curve represents the density of the aqueous phase with zero CO<sub>2</sub> concentration, and the end point of each curve represents the density of CO<sub>2</sub> saturated aqueous solution at the corresponding pressure. These results indicated that the density of aqueous CO<sub>2</sub> solution at a given pressure increased linearly with CO<sub>2</sub> concentration for both CO<sub>2</sub> + deionized water and CO<sub>2</sub> + brine systems. In each system, all the curves of different pressures had the same slope,  $\beta$ , within the experimental errors. The slope for CO<sub>2</sub> + deionized water ( $\beta = 8.456 \text{ g}\cdot\text{mol}^{-1}$ ) was a bit higher than that for CO<sub>2</sub> + brine ( $\beta = 6.738 \text{ g}\cdot\text{mol}^{-1}$ ). Similarly, Ohsumi et al.<sup>2</sup> observed a linear relationship between the density increase and CO<sub>2</sub> concentration in their measurements for CO<sub>2</sub> + seawater. On the basis of the relationship shown in Figures 5 and 6, the density of aqueous CO<sub>2</sub> solutions can be calculated by

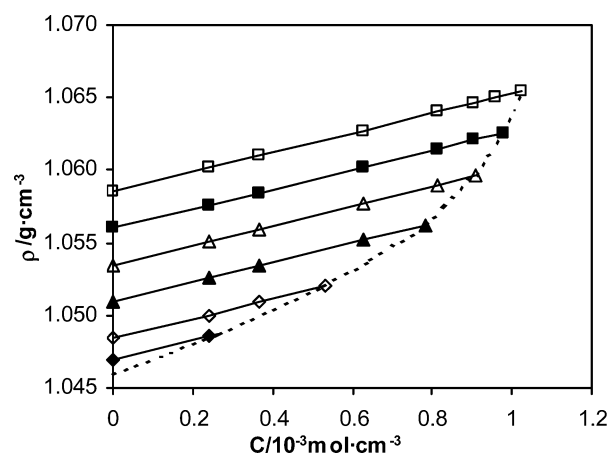
$$\rho/(\text{g}\cdot\text{cm}^{-3}) = \rho_p/(\text{g}\cdot\text{cm}^{-3}) + \beta/(\text{g}\cdot\text{mol}^{-1})C/(\text{mol}\cdot\text{cm}^{-3}) \quad 0 \leq C \leq C_{\text{sat}} \quad (11)$$

where  $\rho_p$  is the density of the aqueous phase with zero CO<sub>2</sub>





**Figure 5.** Density of CO<sub>2</sub> + deionized water vs CO<sub>2</sub> concentration under selected pressures at 59 °C. ◆, 2 MPa; ◇, 5 MPa; ▲, 10 MPa; △, 15 MPa; ■, 20 MPa; □, 25 MPa.



**Figure 6.** Density of CO<sub>2</sub> + Weyburn brine vs CO<sub>2</sub> concentration under selected pressures at 59 °C. ◆, 2 MPa; ◇, 5 MPa; ▲, 10 MPa; △, 15 MPa; ■, 20 MPa; □, 25 MPa.

**Table 7.** Values of Parameters in Equations 11 and 12

	$\beta/(\text{g}\cdot\text{mol}^{-1})$	$\alpha/(10^{-4}\text{ g}\cdot\text{cm}^{-3}\cdot\text{MPa}^{-1})$	$\rho_0/(\text{g}\cdot\text{cm}^{-3})$
deionized water	8.456	5.241	0.9844
Weyburn brine	6.738	5.045	1.0459

concentration at given pressure  $P$ .  $C$  is the concentration of CO<sub>2</sub> in aqueous solution,  $C_{\text{sat}}$  is the CO<sub>2</sub> solubility in aqueous solution at the corresponding pressure  $P$ ,  $\rho$  is the density of CO<sub>2</sub> aqueous solutions at CO<sub>2</sub> concentration  $C$  and pressure  $P$ , and  $\beta$  is the slope of density vs concentration in Figures 5 and 6.  $\rho_p$  is determined by

$$\rho_p = \rho_0 + \alpha P \quad (12)$$

where  $P$  is the pressure and  $\alpha$  is the slope of density vs pressure with zero CO<sub>2</sub> concentration for deionized water or brine, i.e., the slope of the curve with solids diamonds in Figure 3 for CO<sub>2</sub> + deionized water and that in Figure 4 for CO<sub>2</sub> + brine.  $\rho_0$  is the intercept of the curve of density vs pressure at zero CO<sub>2</sub> concentration in Figures 3 and 4 for deionized water and brine, respectively. Values of  $\beta$ ,  $\alpha$ , and  $\rho_0$  for the systems tested in this work are listed in Table 7.

Three parameters  $\beta$ ,  $\alpha$ , and  $\rho_0$  in eqs 11 and 12 may change with the water samples (such as brine at different salinities) and temperature. A simple method for determining the density of aqueous CO<sub>2</sub> solutions can be proposed as follows. The first step is to measure the density of the

aqueous phase with zero CO<sub>2</sub> concentration as a function of pressure to find  $\rho_0$  and  $\alpha$  in eq 12. The second step is to measure densities of aqueous CO<sub>2</sub> solution at a constant pressure but different CO<sub>2</sub> concentrations to find the value of  $\beta$ . Then apply eqs 11 and 12 for the same CO<sub>2</sub> + water system to calculate the density of aqueous CO<sub>2</sub> solution as a function of CO<sub>2</sub> concentration and pressure at a constant temperature.

## Conclusions and Recommendations

Solubilities of CO<sub>2</sub> in deionized water and brine and densities of CO<sub>2</sub> + deionized water and CO<sub>2</sub> + brine solutions were measured at a temperature of 59 °C and pressures up to 29 MPa. It was found that: (1) The dissolution of CO<sub>2</sub> in both deionized water and brine increases the density of aqueous phase. (2) For a constant CO<sub>2</sub> concentration, the density of an aqueous CO<sub>2</sub> solution increases linearly with pressure. For the same CO<sub>2</sub>-aqueous system and at a constant temperature, the slopes of density vs pressure curves for different CO<sub>2</sub> concentrations are the same. (3) Similarly, for a constant pressure, the density of an aqueous CO<sub>2</sub> solution increases linearly with CO<sub>2</sub> concentration. For the same CO<sub>2</sub>-aqueous system and at a constant temperature, the slopes of density vs concentration curves for different pressures are the same. (4) The Chang et al.<sup>15</sup> correlation can provide a good prediction for CO<sub>2</sub> solubility in the deionized water and brine.

A correlation for density of aqueous CO<sub>2</sub> solutions was presented based on the results of this work. A simple method for determining the density of aqueous CO<sub>2</sub> solutions was recommended.

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